

1 **Skillful Empirical Subseasonal Prediction of Landfalling**
2 **Atmospheric River Activity using the Madden-Julian Os-**
3 **cillation and Quasi-Biennial Oscillation**

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6 **Abstract**

7 Upon landfall, atmospheric rivers (ARs)—plumes of intense water vapor transport—often trigger
8 weather and hydrologic extremes. Presently, no guidance is available to alert decision makers to
9 anomalous AR activity within the subseasonal time scale (approximately 2–5 weeks). Here, we
10 construct and evaluate an empirical prediction scheme for anomalous AR activity based solely
11 on the initial state of two prominent modes of tropical variability: the Madden-Julian oscillation
12 (MJO) and the quasi-biennial oscillation (QBO). The MJO—the dominant mode of intraseasonal
13 variability in the tropical troposphere—modulates landfalling AR activity along the west coast of
14 North America by exciting large-scale circulation anomalies over the North Pacific. In light of
15 emerging science regarding the modulation of the MJO by the QBO—the dominant mode of in-
16 terannual variability in the tropical stratosphere—we demonstrate that the MJO–AR relationship
17 is further influenced by the QBO. Evaluating the prediction scheme over 36 boreal winter seasons,
18 we find skillful subseasonal “forecasts of opportunity” when knowledge of the MJO and the QBO
19 can be leveraged to predict periods of increased or decreased AR activity. Certain MJO and QBO
20 phase combinations provide empirical subseasonal predictive skill for anomalous AR activity that
21 exceeds that of a state-of-the-art numerical weather prediction model. Given the wide-ranging im-
22 pacts associated with landfalling ARs, even modest gains in the subseasonal prediction of anoma-
23 lous AR activity may support decision making and benefit numerous sectors of society.

24 **Keywords:** subseasonal prediction, atmospheric river, teleconnection, Madden-Julian oscillation

25 **1 Introduction**

26 A comparative gap in forecast guidance exists between medium-range weather forecasts (up to
27 2 weeks) and seasonal outlooks (3+ months)¹⁻³. Thus, opportunities abound to add far-reaching
28 value to society with skillful predictions of extreme, and frequently hazardous, weather events
29 that occur within this so-called subseasonal-to-seasonal gap³. Sectors such as agriculture, energy
30 production, resource management, and insurance stand to benefit from advance notice of weather
31 extremes in order to prepare for such events.

32 Here, we focus on the subseasonal time scale that spans forecast lead times of approximately
33 2–5 weeks. Skillful predictions of extratropical phenomena within this time scale generally rely on
34 the prediction of large-scale circulation anomalies⁴, which are often linked to tropical disturbances
35 that excite quasi-stationary Rossby waves that propagate into the extratropics⁵⁻⁷. Indeed, predic-
36 tive power in the subseasonal time scale is largely associated with the evolution of far-reaching
37 teleconnections produced by tropical phenomena such as the Madden-Julian oscillation (MJO)^{8,9}.
38 The MJO is the dominant mode of intraseasonal variability in the tropical troposphere and is often
39 characterized by a large-scale pattern of coupled anomalous atmospheric circulation and deep con-
40 vection that propagates eastward along the equator with a period of approximately 30–90 days¹⁰.
41 Additionally, the MJO is known to be an important source of subseasonal predictability^{9,11,12} and
42 can support predictions of various phenomena outside of the tropics. For example, a recently devel-
43 oped empirical model for predicting North American 2-meter temperatures based on the MJO, the
44 El Niño-Southern Oscillation (ENSO) cycle, and linear trends produces skill and provides valuable

45 guidance beyond a basic climatological forecast¹³. Moreover, the teleconnection patterns associ-
46 ated with the ENSO cycle and the MJO provide a scientific basis for subseasonal prediction with
47 operational forecast models¹⁴.

48 Emerging science is illuminating the influence that the state of the tropical stratosphere has
49 on the MJO and its teleconnections. Here, the state of the stratosphere is represented by the phase
50 of the quasi-biennial oscillation (QBO). The QBO is the dominant mode of the variability in the
51 tropical stratosphere and is itself highly predictable¹⁵. The QBO represents a downward propagat-
52 ing shift in the mean zonal winds in the equatorial stratosphere from westerlies to easterlies and
53 back again, with a period of approximately two years¹⁶. A growing body of research suggests that
54 the state of the stratosphere, as represented by the QBO, influences the nature and predictability
55 of the MJO^{17,18}, as well as the MJO's associated atmospheric teleconnections^{18,19}. For example,
56 MJO activity during boreal winter is generally higher in amplitude and slower to propagate during
57 the easterly phase of the QBO than during the westerly phase^{17,19-21}. This modulation of the MJO
58 by the QBO can occur independent of the ENSO cycle^{17,19,21}. While the physical processes re-
59 sponsible for the modulation of the MJO by the QBO are still being investigated, the relationship
60 appears to be dominated by the regulation of the near-tropopause temperature and static stability
61 and hence a modulation of organized deep convection^{17,21}.

62 In this work, we construct and evaluate an empirical prediction scheme targeting anoma-
63 lous landfalling atmospheric river (AR) activity along the west coast of North America. ARs are
64 plumes of intense tropospheric water vapor transport that often result in weather and/or hydro-

65 logic extremes (e.g., heavy rainfall, flash floods) upon landfall^{22–25}. Repeated landfalling ARs or
66 a complete lack thereof may result in periods of precipitation abundance or drought for regions
67 along the west coast of North America^{26,27}. Several studies suggest the potential for skillful sub-
68 seasonal prediction based on observed relationships between the MJO and AR activity^{28–32}. Here,
69 we show that knowledge of the state of the MJO and the QBO can provide skillful predictions of
70 anomalous AR activity up to 5 weeks in advance during boreal winter months. Because of the
71 wide-ranging impacts associated with landfalling ARs, myriad sectors of society may benefit from
72 skillful predictions of anomalous AR activity along the west coast of North America.

73 **2 Results**

74 ARs impact the west coast of North America during every month of the year³². However, re-
75 gions along the coast experience a pronounced seasonality in AR frequency of occurrence that
76 generally varies with latitude^{33,34}. The landfall boundaries used in this study, as identified in Fig-
77 ure 1a, are no exception. Figure 1b shows the seasonal cycle of landfalling ARs near British
78 Columbia (BC; blue) and California (CA; red) based on ARs identified in the second Modern-
79 Era Retrospective Analysis for Research and Applications (MERRA-2) dataset³⁵ (results for the
80 Alaska and Washington/Oregon landfall boundaries are provided in the Supplementary Informa-
81 tion). We focus our analysis on the December through March (DJFM) period, as shaded in Figure
82 1b, when ARs frequently occur near both the British Columbia and California landfall bound-
83 aries, when teleconnection patterns are expected to be the most robust over the North Pacific, and
84 when the aforementioned MJO–QBO link has been observed. In Figure 1b, ARs occur at frequen-

85 cies of approximately 12.4% and 11.5% of all days during DJFM for the British Columbia and
86 California boundaries, respectively. Not shown is the substantial year-to-year variability in AR
87 occurrences^{32,34} indicating that landfalling ARs are also influenced by longer time scale modes of
88 variability such as the ENSO cycle.

89 AR activity near these landfall boundaries not only varies on seasonal and longer time scales,
90 but also within the subseasonal time scale. Here, we assess the modulation of AR activity following
91 periods when the MJO is active. The MJO is parsed into eight phases that relate to the approximate
92 location of the anomalous convection associated with the MJO, according to the components of
93 the real-time multivariate MJO (RMM) index³⁶ (see Methods). Figure 2 depicts anomalous AR
94 frequency of occurrence following dates when the MJO is active in a given phase, based on the 36
95 DJFM seasons (1980–2016) within the MERRA-2 record. These composite anomalies may also
96 be thought of in terms of percent change relative to the aforementioned 12.4% and 11.5% DJFM
97 mean AR frequencies for British Columbia and California, respectively. As such, Figure 2 reveals
98 composite patterns of anomalous AR activity following certain MJO phases that approach, or even
99 exceed, +/- 50% of the seasonal AR frequency of occurrence. The opposing anomaly patterns
100 in Figure 2 also capture a tradeoff in AR activity between British Columbia and California. For
101 example, the increase in AR activity near British Columbia approximately two weeks following
102 MJO phase 2 contrasts with a simultaneous decrease in activity near California (see also ref. 34).

103 In addition to the modulation of AR activity following active MJO periods, Figure 2 cap-
104 tures some key characteristics of the MJO and its extratropical response. For example, the angled,

105 alternating pattern of anomalous AR activity captures the eastward propagation of the canonical
106 MJO signal. Additionally, Figure 2 reveals that the maximum MJO-related impacts may take sev-
107 eral days, or even weeks, to manifest, in agreement with the results of earlier theoretical work^{7,37}.
108 Notably, these patterns emerge despite the high degree of variability (duration, strength, evolution,
109 etc.) within the underlying MJO events.

110 Despite the revealing patterns in Figure 2, such an analysis does not assess whether the
111 modulation of AR activity following MJO activity is of use in a predictive sense. Here, we develop
112 an empirical prediction scheme to evaluate the predictive potential of the MJO–AR relationship. In
113 this first version of the scheme, the predictor is the initial state of the MJO, represented simply by
114 the numeric MJO phase on the date of forecast issuance. The predictand is anomalous AR activity
115 at some date in the future (i.e., forecast lead) near a given landfall boundary. While others have
116 evaluated the ability of medium-range weather forecasts to represent individual AR events³⁸, we
117 target periods of AR activity relative to the seasonal cycle and smoothed by a 5-day running mean
118 (see Methods). This particular choice of predictand transforms the transient, synoptic-scale nature
119 of individual ARs into a broader representation of the propensity of the large-scale flow pattern
120 to support anomalous AR activity (i.e., increased or decreased activity relative to the seasonal
121 climatology) and is a more suitable target for subseasonal prediction.

122 Using a leave-one-out cross-validation training and verification approach, we verify the pre-
123 diction scheme on all DJFM dates for forecast lead times spanning 2 to 36 days. Forecast leads are
124 defined as the number of days between the initial conditions (i.e., when forecasts are made) and

125 the verification dates (i.e., the dates for which AR activity is forecast). Thus, MJO conditions as
126 early as late October are used as predictors. The Heidke skill score (HSS; see Methods) is used
127 to quantify the value added by this prediction scheme. As constructed, the HSS ranges from -100
128 (no correct forecasts) to 100 (all forecasts are correct), and HSS values greater than zero indicate
129 conditions when the scheme adds value compared to a climatological forecast.

130 Figure 3 depicts the skill of the empirical prediction scheme as a function of MJO phase and
131 forecast lead time for the British Columbia and California landfall boundaries. The panels in Figure
132 3 are shaded where the HSS is positive, that is, where skill emerges from this empirical prediction
133 scheme (see Supplementary Figure S6 for a plot of the full range of scores comparable to Figure
134 3a–b). The extent of the shading in Figure 3a–b reveals that the MJO–AR relationship provides
135 useful information within the subseasonal time scale beyond a simple climatological forecast. For
136 context, an HSS value of 33 means that there are twice as many correct forecasts as incorrect
137 forecasts. The color of the shading in Figure 3 relates to the AR response, with orange shading
138 for decreased AR activity and green shading for increased AR activity. The skillful response
139 patterns in Figure 3a–b share some similarities with the composite patterns shown in Figure 2. For
140 example, the band of anomalously high AR activity near British Columbia following MJO phases
141 1–6 in Figure 2a supports skillful predictions of increased AR activity following the same phases
142 in Figure 3a. Additionally, the patterns of skillful predictions suggest that the composites in Figure
143 2 are not dominated by just a few outlier events, but rather capture robust shifts in AR activity due
144 to the state of the MJO up to 5 weeks prior.

145 Inspired by recent work investigating the impacts of the QBO on the MJO, we repeat our
146 predictions but now include the phase of the QBO as an additional predictor. In Figure 3, pan-
147 els c–f follow the format of panels a–b, but are parsed according to QBO phase: easterly QBO
148 (EQBO) and westerly QBO (WQBO). As an example, the streak of statistically significant skill for
149 increased AR activity near British Columbia during EQBO conditions and 18–26 days following
150 MJO phase 1 (bottom row of Figure 3c) indicates that given the initial conditions of EQBO and
151 active MJO phase 1, one should expect an increase in AR activity relative to the seasonal clima-
152 tology approximately three weeks following. The skill metric suggests that such a prediction of
153 increased AR activity would be correct approximately 20 times out of 30. We also find that when
154 the prediction scheme adds value ($HSS > 0$), the skill is often higher with the addition of the QBO
155 as a predictor. While some of the general skill and response patterns from the “QBO independent”
156 panels remain once parsed by QBO phase, it is apparent that the patterns of anomalous AR activity
157 in Figure 3a–b are generally dominated by different phases of the QBO. For example, the band
158 of increased AR activity near British Columbia 1–3 weeks following MJO phases 1–3 is most
159 pronounced during EQBO conditions.

160 To learn more about the dynamics that contribute to the AR response patterns shown in Fig-
161 ure 3, we examine composites of integrated water vapor transport (IVT) and 500 hPa geopotential
162 height anomalies over the North Pacific. The large-scale anomaly patterns reveal conditions that
163 act to influence AR activity near the landfall boundaries. Perhaps not surprisingly, the more skill-
164 ful the prediction scheme (i.e., higher and more significant HSS), the more coherent the associated
165 anomaly patterns appear over the North Pacific. For example, conditional composites for 18 days

166 following MJO phase 1 dates during easterly and westerly QBO conditions are shown in Figures
167 4a and 4b, respectively. In Figure 4a, a negative height anomaly centered over mainland Alaska
168 contrasts with a broad positive height anomaly encompassing much of the North Pacific. These
169 anomaly patterns favor anomalously high AR activity near British Columbia and low AR activ-
170 ity near California. The anomaly patterns are less pronounced during westerly QBO conditions
171 (Figure 4b), but the associated AR activity impacts are of the same sign regardless of QBO phase.
172 In contrast, panels c–d of Figure 4 show composite conditions for 12 days following MJO phase
173 5 dates with dissimilar extratropical anomaly patterns when parsed by QBO phase and with the
174 composite anomaly pattern appearing substantially weaker and less coherent in the easterly QBO
175 phase. In both panels, the composite height and IVT anomaly patterns are conducive for an AR
176 activity tradeoff between the two landfall boundaries³⁴. Overall, the example composites shown
177 in Figure 4 highlight that the anomalous AR response patterns (e.g., Figure 3) are linked to the
178 large-scale modulation of the extratropical circulation.

179 A worthwhile question is how does the level of skill from this empirical prediction scheme
180 compare to the skill available from numerical weather prediction models? To answer this question,
181 we evaluate a suite of 46-day European Centre for Medium-Range Weather Forecasts (ECMWF)
182 retrospective forecasts initialized from 1995 to 2016². As with the empirical method, we target
183 5-day average anomalous AR activity for each landfall boundary. Figure 5 shows the resulting
184 HSS based on all verification dates in DJFM as a function of forecast lead time for both the British
185 Columbia (blue) and California (red) landfall boundaries. The ECMWF ensemble prediction sys-
186 tem shows skill initially; however, the skill decreases to near zero at approximately 18 days. Thus,

187 the model's subseasonal skill with this metric is roughly equivalent to a climatological forecast
188 beyond forecast lead times of 18 days. The HSS values plotted in Figure 5 are not parsed by MJO
189 and QBO phase; however, as shown in the Supplementary Information's Figures S10 and S11, the
190 results do not vary remarkably when the initial state of the MJO and the QBO are considered. This
191 brief assessment is not intended to be a critique of this particular model, but rather to provide a
192 rough estimate of the ability of a current generation numerical weather prediction model to predict
193 anomalous AR activity within the subseasonal time scale.

194 **3 Discussion**

195 This study illuminates the predictive potential of the relationship between anomalous landfalling
196 AR activity along the west coast of North America and the state of the tropics up to 5 weeks
197 prior. Earlier works have documented an MJO–AR relationship in terms of the modulation of AR
198 occurrences^{30–32} and their impacts²⁹, but here we demonstrate that the time-lagged modulation of
199 AR activity by the extratropical response to the MJO can be leveraged for skillful subseasonal
200 forecasts. We further show that the MJO–AR relationship is influenced by the QBO. Thus, the
201 variability of the MJO–AR relationship can be better understood and predicted by also considering
202 the state of the stratosphere. Furthermore, key aspects of the skill and AR response patterns are
203 generally robust to the indices and thresholds used to characterize the MJO and the QBO (see
204 Supplementary Information).

205 An empirical prediction scheme using the initial state of the MJO and the QBO as predictors

206 can support skillful subseasonal “forecasts of opportunity.” As shown, during certain phase com-
207 binations (i.e., MJO phase, QBO phase, and forecast lead) the prediction scheme produces skill
208 at forecast lead times of 2–5 weeks exceeding that of a state-of-the-art numerical weather predic-
209 tion model, when evaluated using a similarly-constructed metric for above and below normal AR
210 activity. Our scheme could be operationalized in such a manner as to revert to climatology if no
211 additional skill can be expected, thus affording continuous application to complement available
212 numerical weather prediction guidance. Furthermore, the method could be married with predic-
213 tions of the MJO itself, predictions which now show skill out 3–4 weeks in some dynamic models
214 and situations^{39–41}.

215 As ARs can trigger wide-ranging impacts, even modest gains in the subseasonal prediction of
216 these impactful features may benefit numerous sectors of society. Also significant is the result that
217 the MJO–AR relationship is responsible for not only periods of increased landfalling AR activity,
218 but also periods of decreased activity. Given the potential consequences of a lack of AR activity,
219 inactive periods may be just as viable and valuable a predictive target as abnormally active periods.
220 Whatever the response, this study elucidates key relationships that contribute to the subseasonal
221 variability of these extreme events and support skillful predictions thereof.

222 **4 Methods**

223 **Atmospheric river detection.** ARs are identified using an updated version of an objective detec-
224 tion algorithm (as documented in ref. 32). The algorithm uses gridded fields of positive anomalous

225 vertically integrated water vapor transport (IVT), together with a series of intensity and geometric
226 tests (e.g., mean intensity, total area, length, length-to-width ratio), to identify features that are
227 of the appropriate spatial scale and are sufficiently plumelike in nature. This detection algorithm
228 employs an occurrence-based approach (i.e., an AR occurrence is recorded for each period during
229 which the criteria are satisfied), wherein each time step is scrutinized independently. As a result,
230 the calculations regarding AR “hits” described in this study are based on the number of days during
231 which AR-like conditions exist over a given landfall boundary. The updated detection algorithm
232 used in this study does not contain the “multiple peak” logic that scrutinizes connected features
233 within fields of anomalous IVT. We find that the mid- and high-latitude results are generally in-
234 sensitive to the removal of this logic test. The majority of the results presented in this work are
235 based on this detection algorithm applied to IVT calculated via the mass-weighted vertical integra-
236 tion of component winds and specific humidity from 1000-250 hPa from the second Modern-Era
237 Retrospective Analysis for Research and Applications (MERRA-2)³⁵. Daily means are calculated
238 and the dataset is regridded to a $1.5^\circ \times 1.5^\circ$ latitude-longitude grid before calculating IVT. With
239 this dataset, a static anomalous IVT magnitude threshold of $\sim 173 \text{ kg m}^{-1} \text{ s}^{-1}$ is used to isolate
240 features of interest. This value represents the 94th percentile of the all-season distribution of daily
241 IVT anomaly values over the North Pacific Ocean. For the model skill comparison, this AR de-
242 tection scheme is also applied to gridded IVT anomalies calculated from a set of retrospective
243 forecasts from the European Centre for Medium-Range Weather Forecasts (ECMWF) reforecast
244 ensemble prediction system.

245 **Atmospheric river activity.** To construct time series of anomalous AR activity along the landfall
246 boundaries, we first create a continuous time series of boolean AR “hits” for each boundary by
247 recording a hit whenever the spatial extent of any AR feature overlaps at least one grid point of
248 a given landfall boundary. Second, we remove the seasonal cycle of AR activity by subtracting
249 the mean and first two harmonics calculated via fast Fourier transform applied to the calendar-day
250 means of each AR time series. Third, we apply a 5-day running mean to each anomaly time series.
251 Based on the premise that subseasonal predictions are founded on the presence and modulation of
252 large-scale circulation anomalies, the running mean transitions the time series from representing
253 only individual transient hits to capturing the larger-scale propensity of the anomalous flow pattern
254 to influence the landfalling activity. The resulting time series are used to create the conditional
255 composites for Figure 2 and to train and verify the prediction scheme described throughout this
256 work.

257 **Predictors.** Two potential sources of subseasonal predictability are used as initial conditions for
258 the prediction scheme: the MJO and the QBO. We characterize the MJO according to the strength
259 and location of the enhanced near-equatorial convection and the associated anomalous circula-
260 tion, as determined by the components of the real-time multivariate MJO (RMM) index³⁶. This
261 MJO index is a combination of two component indices, RMM1 and RMM2, representing the two
262 leading principal components from a multivariate (equatorially averaged tropical outgoing long-
263 wave radiation and 200- and 850-hPa zonal winds) empirical orthogonal function analysis. When
264 combined and considered in terms of their two-dimensional phase space, these component indices
265 provide daily phase (1–8) and amplitude values (see ref. 36). We consider the MJO as active when

266 the amplitude meets or exceeds a value of one and also apply the basic logic test that the index
267 must remain in that phase (e.g., location of active MJO signal) for at least two, but less than 20,
268 days. See the Supplementary Information for alternative characterizations of the MJO (e.g., dif-
269 ferent index or more stringent phase event criteria). The QBO is characterized by the standardized
270 monthly 50 hPa zonal wind index provided by the National Oceanic and Atmospheric Administra-
271 tion (NOAA) National Weather Service (NWS) Climate Prediction Center (CPC). We apply this
272 index as a continuous time series, such that all months within the period of record are categorized
273 as either EQBO (monthly mean standardized anomaly <0) or WQBO (>0). We show the impact
274 of introducing a more restrictive anomaly threshold, which has the possible effect of bolstering
275 the prediction scheme, but also reducing the number of conditional samples, in the Supplementary
276 Information's Figure S13. The QBO is not considered alone based on the presumption that the
277 influence of the QBO on anomalous AR activity will primarily manifest via the modulation of the
278 MJO's convection and its ability to elicit an extratropical response. Hence, the predictors investi-
279 gated in this study are simply the daily MJO phase (1–8) and the monthly QBO phase (EQBO or
280 WQBO).

281 **Empirical prediction.** We generate a two-class prediction scheme from the DJFM AR anomaly
282 time series for each region; that is, we assess the probability of being above and the probability of
283 being below an “equal chances” 50th percentile of the time series given the initial state of the MJO
284 and the QBO. As constructed, the probability of being above (increased AR activity) and below
285 (decreased AR activity) are equal when all verification dates in DJFM are considered. However,
286 the probability distribution may shift as a function of MJO phase, QBO phase, and forecast lead.

287 For the example shown in Supplementary Figure S5, the distribution of 5-day average anomalous
288 AR activity near British Columbia is shifted toward higher values 18 days following MJO phase 1
289 dates during EQBO conditions, relative to the mean DJFM distribution. As a result, given the ini-
290 tial conditions of MJO phase 1 and EQBO, the empirical scheme will predict increased AR activity
291 for the British Columbia landfall boundary around 18 days following these initial conditions. In
292 evaluating the two-class scheme, a prediction is considered correct when the observed response, in
293 terms of above or below the 50th percentile threshold, from the 5-day running mean of the indepen-
294 dent verification time series matches the predicted response; the prediction is considered incorrect
295 otherwise. As illustrated by this example, the predictors are not explicitly weighted as they may be
296 in a scheme based on some form of regression; in contrast, the predictors (MJO phase and QBO
297 phase) are simply used to parse the training data in order to assess the conditional shift in the like-
298 lihood of increased or decreased AR activity relative to seasonal climatology. Though the results
299 presented herein are based on the use of a single DJFM 50th percentile threshold, we find that the
300 overarching conclusions (time-lagged response, patterns of increased/decreased AR activity, etc.)
301 remain even if the threshold is allowed to vary by day-of-season. We use a leave-one-out cross-
302 validation approach to conditionally construct and evaluate this prediction scheme⁴². Specifically,
303 the verification statistics for a given season are based on distributions constructed from historical
304 AR activity parsed by phase of the MJO and the QBO for all DJFM seasons excluding the one “left
305 out” verification season, ensuring independence of the verification subset. As a given season is left
306 out, we use the training data to generate forecasts for all 121 days within the left out season and
307 for all possible forecast leads. In so doing, we perform this leave-one-out procedure 36 times, each

308 time leaving out just one DJFM season from the available MERRA-2 record. Because the training
309 periods differ during the leave-one-out process, the 50th percentile threshold is recalculated each
310 time; however, the threshold value is nearly unchanged throughout the cross-validation. The out-
311 put of the cross-validation procedure is the number of correct and incorrect predictions parsed by
312 initial conditions and forecast lead times.

313 **Skill assessment.** The skill of the prediction scheme is evaluated using the Heidke Skill Score
314 (HSS), a measure of the proportion of correct forecasts^{13,42}. The HSS is calculated as:

$$315 \quad HSS = \frac{(H - E)}{(T - E)} \times 100, \quad (1)$$

316 where H is the number of correct forecasts, T is the total number of forecasts evaluated, and E
317 is the number of correct forecasts expected by chance ($T/2$ in this two-class scenario). With the
318 multiplication by 100, the two-class HSS ranges from -100 to 100. A set of perfect forecasts
319 garners a HSS of 100, forecasts equivalent to the reference forecast (i.e., climatology) score 0, and
320 forecasts less skillful than the reference forecast receive negative scores. The HSS values may be
321 interpreted in terms of value added relative to a climatological reference forecast. For example, a
322 HSS of 33 indicates twice as many correct forecasts as incorrect forecasts and a skill score of 50
323 indicates three times as many correct as incorrect forecasts; whereas, the reference forecast with a
324 skill score of 0 indicates an equal number of correct and incorrect forecasts.

325 **Significance of skill.** A block bootstrapping approach is used to assess the statistical significance
326 of the HSS values. For every conditional combination (i.e., MJO phase, QBO phase, and forecast
327 lead), we generate a distribution of 1000 skill score values by randomly reassigning the calendar

328 year and shifting the day-of-year indices of the “blocks” of the occurrences of the conditional data.
329 We then perform the verification calculations on the random data in order to construct a distribution
330 of resampled HSS values against which the actual conditional HSS may be compared. In doing so,
331 each block bootstrap sample retains the sample size and potential autocorrelation associated with
332 the conditional data.

333 **Atmospheric river response assessment.** For Figure 3 and the associated discussion we aim to
334 not only communicate the skill within the prediction scheme, but also characterize the conditional
335 AR response. To achieve this, we evaluate the shift in the probability of above and below normal
336 AR activity for each conditional combination throughout the leave-one-out training and verifica-
337 tion process. For example, if a given MJO phase, QBO phase, and forecast lead combination
338 consistently produces a probability of above normal AR activity greater than the probability of be-
339 low normal activity, we record the condition as resulting in above normal, or increased, AR activity
340 and shade the combination green in Figure 3.

341 **Model skill comparison.** In order to provide a numerical weather prediction skill benchmark, we
342 calculate HSS values for a set of 46-day ECMWF retrospective forecasts from 1995-2016. The
343 ECMWF reforecast ensemble prediction system dataset consists of 11 members (one control and
344 ten perturbed) that are created “on-the-fly.” That is to say that the database is comprised of output
345 from different versions of the ECMWF model, as reforecasts are produced progressively as the
346 the operational model is updated². We obtain instantaneous 0000 UTC variables on a $1.5^\circ \times 1.5^\circ$
347 latitude-longitude grid, from which we calculate IVT and identify AR-like features. We use the

348 first 7 days from every available control run reforecast to calculate calendar-day means from which
349 we calculate the seasonal cycle via fast Fourier transform. Time series of anomalous AR activity
350 are created for each ensemble member's reforecasts by removing the control run's seasonal cycle
351 and applying a 5-day running mean. The 50th percentile threshold used to evaluate AR activity is
352 based on anomalies from the control run, subset for the boreal winter. Each member is evaluated
353 separately and for all verification dates within DJFM. Following this approach, 1919 reforecasts
354 are used.

355 **Data availability.** MERRA-2 data were obtained from the NASA Goddard Earth Sciences Data
356 and Information Services Center (<https://disc.gsfc.nasa.gov/>). ECMWF reforecast
357 ensemble system output was acquired from the World Weather Research Programme/World Cli-
358 mate Research Programme Subseasonal-to-Seasonal Prediction Project database² (<http://apps.ecmwf.int/datasets/data/s2s/>). The QBO index was provided by the NOAA NWS
359 CPC (<http://www.cpc.ncep.noaa.gov/data/indices/qbo.u50.index>). MJO in-
360 dices were obtained from the Australian Bureau of Meteorology (<http://www.bom.gov.au/climate/mjo/>) and NOAA Earth System Research Laboratory (<https://www.esrl.noaa.gov/psd/mjo/mjoindex/>).

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370 methods and the interpretation of the results. C.F.B obtained and processed the ECMWF reforecast output.
371 B.D.M. drafted the manuscript and all authors contributed to preparing the final version for publication.

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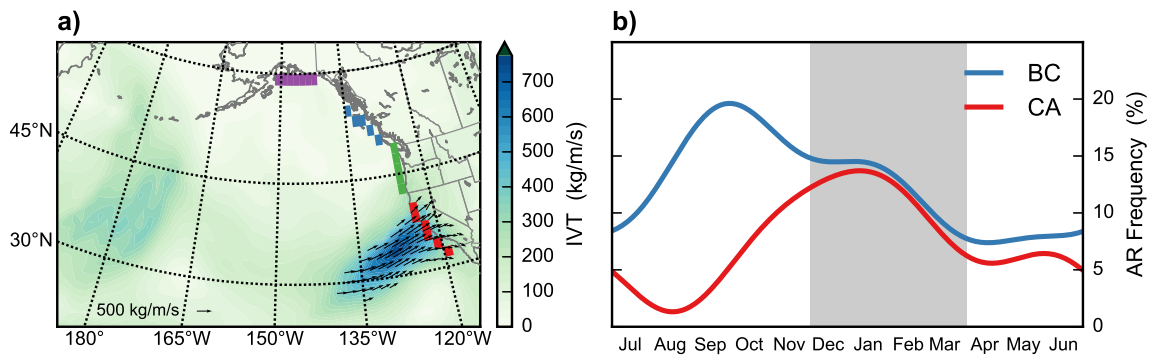


Figure 1: (a) Location of the Alaska (purple), British Columbia (BC; blue), Washington/Oregon (green), and California (CA; red) landfall boundaries overlaying the daily mean integrated water vapor transport (IVT; shaded) from 20 February 2017. The black IVT vectors highlight an AR that impacted the CA boundary on that date. (b) The seasonal cycle of AR frequency of occurrence for the BC (blue curve) and CA (red curve) landfall boundaries, with the December–March (DJFM) period shaded.

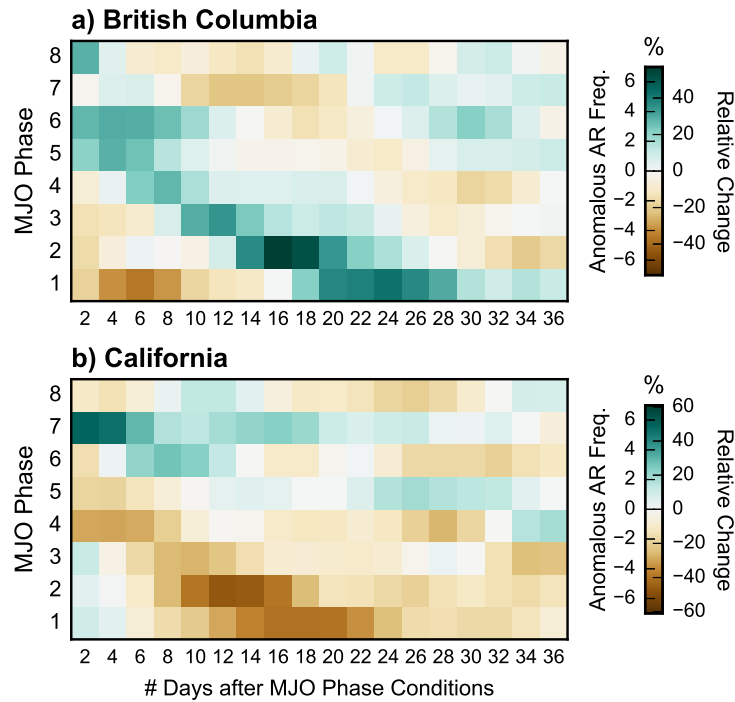


Figure 2: Composite anomalous AR activity as a function of MJO phase (y axis) and number of days after active MJO phase conditions (x axis) in terms of anomalous frequency of occurrence (% , left range of colorbar) and the change relative to the location's mean DJFM AR frequency (% change, right range of colorbar) for the (a) British Columbia and (b) California landfall boundaries.

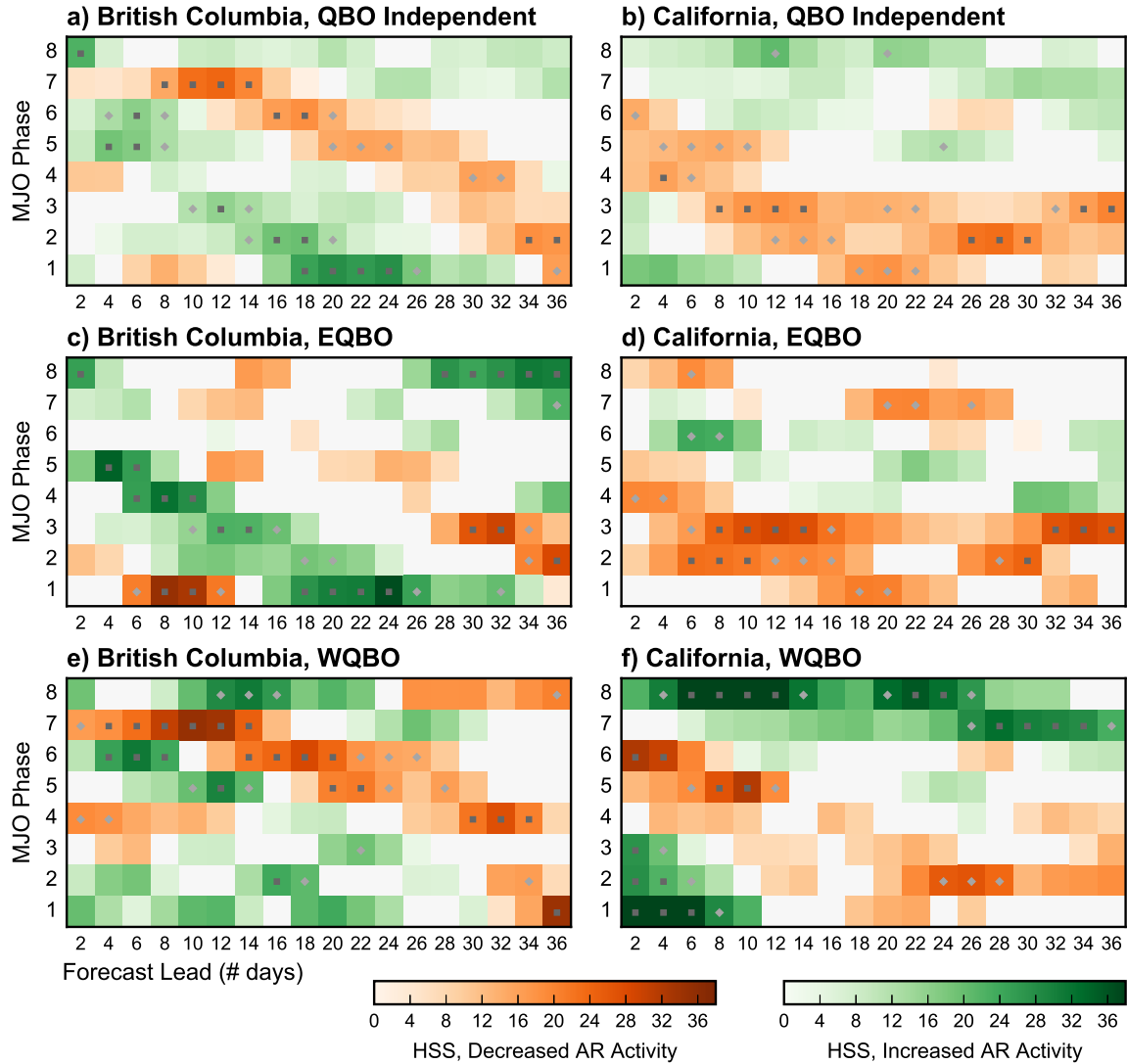


Figure 3: Heidke skill score (HSS) values as a function of MJO phase (y axis) and forecast lead time (x axis) for the British Columbia (left column) and California (right column) landfall boundaries, (a–b) independent of the state of the QBO, as well as conditioned on (c–d) EQBO and (e–f) WQBO. Only conditional combinations where the HSS is positive are shaded. The shading is based on the dominant AR activity response: decreased activity (oranges) or increased activity (greens). Statistical significance of the skill scores is denoted by the light gray diamonds (≥ 80 th percentile) and dark gray squares (≥ 90 th percentile), based on 1000 block bootstrap samples (see Methods).

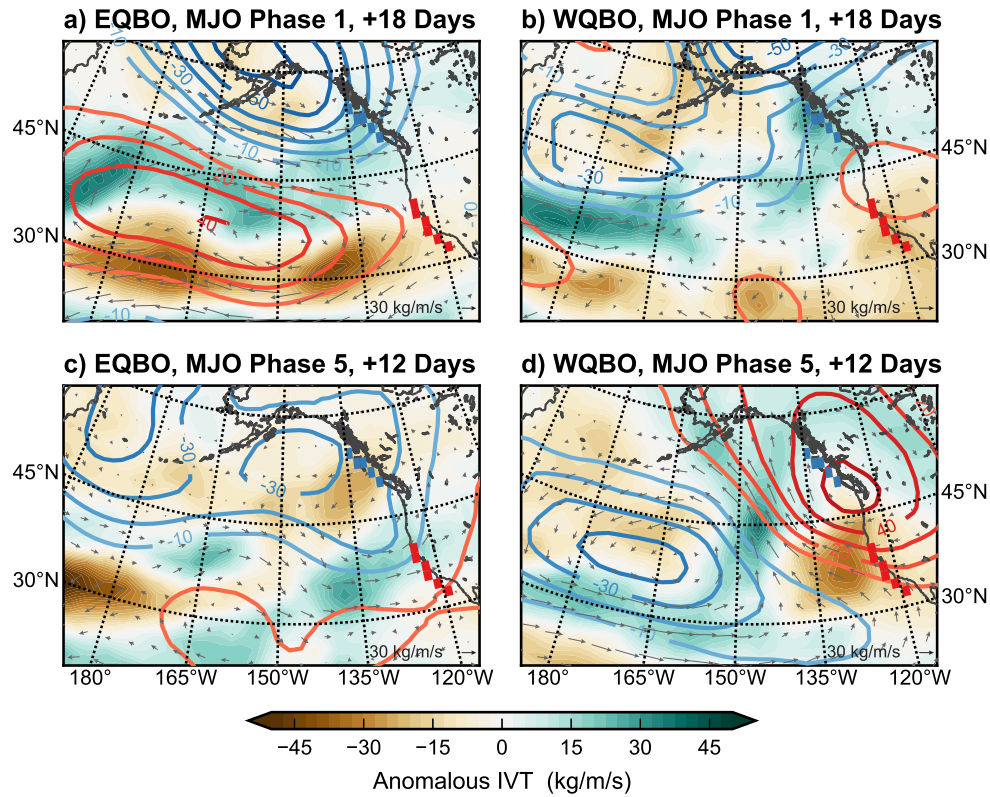


Figure 4: Composites of anomalous integrated water vapor transport (IVT; shaded and arrows), positive 500 hPa geopotential height anomalies (red contours), and negative 500 hPa geopotential height anomalies (blue contours) for (a) 18 days following DJFM MJO phase 1 dates during EQBO conditions, (b) 18 days following MJO phase 1 dates during WQBO, (c) 12 days following MJO phase 5 dates during EQBO, and (d) 12 days following MJO phase 5 dates during WQBO. The British Columbia (blue) and California (red) landfall boundaries are overlaid.

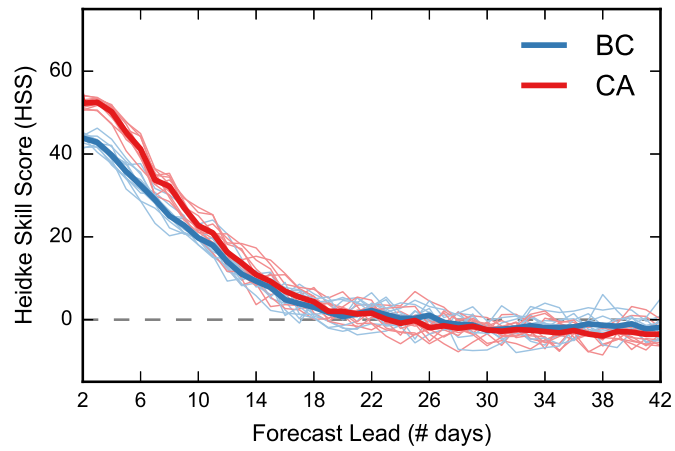


Figure 5: HSS values based on ECMWF reforecast predictions of anomalous AR activity as a function of forecast lead time (x axis) for the British Columbia (BC; blue) and California (CA; red) landfall boundaries. Fine lines represent individual ensemble members and the bold lines denote the mean skill of all ensemble members for each region.